

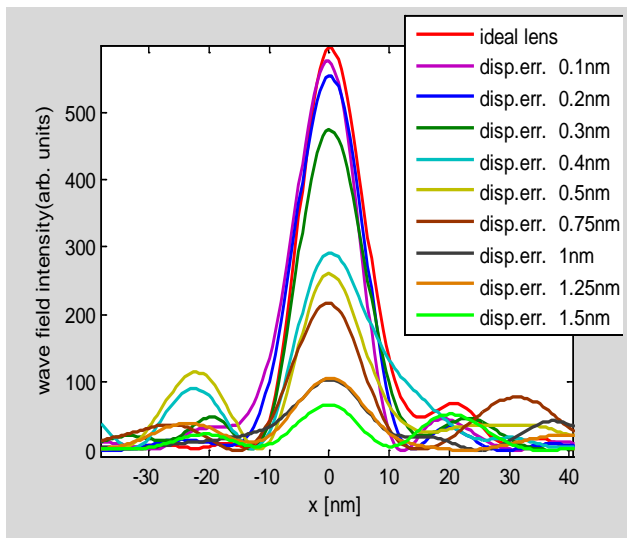
# Numerical Simulation of MLLs with Layer Displacement Error

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The influences of the displacement error of each layers in tilted Multilayer Laue Lens(MLLs) is simulated by Beam Propagation method(BPM)<sup>[1]</sup>. We investigate the convergence of BPM in our cases , then compare the wave field distributions in the output plane and focal plane with the results calculated by Takagi-Taupin description(TTD) of dynamical diffraction theory<sup>[2]</sup>. The two methods coincidence very well. After adding the layer displacement error in the MLLs , the input wave field is propagated through MLLs and to the focal plane. The FWHM and focusing efficiency of the focal spot is presented.



**Fig. 1.**Wave field intensity distribution in the focal plane. The main parameters of the tilted MLL are:  $E=19.5\text{keV}$ ,  $\text{Si/WSi}_2$ ,  $x_{\text{max}}=30\mu\text{m}$ ,  $f=4.72\text{mm}$ ,  $\text{tilt\_angle}=1.6\text{mrad}$

A sequence of displacement error is added to layers in the MLLs. After getting the wave field distribution in the output plane of the focusing lens, We employ Fresnel-Kirchhoff integral<sup>[3]</sup> to calculate the intensity distribution near the focal plane. As expected, the displacement error of layers leads to the decrease of focusing efficiency and a broadening of the focal spot. As the displacement error

can be measured by scanning electron microscope(SEM), We plan to use this simulation method to calculate the wave field distribution behind a real tilted MLL with imperfections.

[1]Thylén. L, *Optical and Quantum Electronics* ,15(5) (1983).

[2] H. F. Yan, J. Maser, A. Macrander, Q. Shen, S. Vogt, G. B. Stephenson, and H. C. Kang, *Phys. Rev. B* **76**, 115438 (2007).

[3] M. Born and E. Wolf, *Principles of Optics*, 7th ed. (Cambridge University Press, Cambridge, 1999).